# Federal Democratic Republic of Ethiopia <br> Ministry of Education 

# Minimum Learning Competencies 

Mathematics, Grades 9 to 12

## Statement of Minimum Learning Competencies (MLCs) in Mathematics for Grade 9 \& 10

| Area of Competency | Grade 9 | Grade 10 |
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| I. NUMBER SYSTEM <br> The real number system | - identify natural numbers and integers <br> - define prime numbers and composite numbers <br> - determine common factors and common multiples of pairs of numbers <br> - show that repeating decimals are also rational numbers <br> - identify irrational numbers <br> - locate some irrational numbers on a number line. <br> - define real numbers. <br> - describe the correspondence between real numbers and points on a numbers line. <br> - Realize the relationship between a power with fractional exponent and a radical form. <br> - Convert powers with fractional exponent to radical form and vice-versa <br> - perform any one of the four operation on the set of real numbers <br> - use the laws of exponents to simplify expression. <br> - give appropriate upper and lower bounds for a given data to a specified accuracy (e.g. rounding off) <br> - express any positive rational number in its standard form. <br> - explain the notion of rationalization. <br> - identify a rationalizing factor for a given expression. <br> - use the Euclid's division algorithm to express given quotients of the form ```p where, p>q. q``` |  |
| II. ALGEBRA <br> Solving Equations and Inequalities | - Solve equations involving exponents and radicals <br> - Solve simultaneous equation <br> - identify the three cases of solutions of simultaneous equations (a unique solution, no solution, infinitely many solutions) <br> - Solve equations involving absolute value <br> - Solve quadratic equations by using any one of the three | - describe sets using internal notation. <br> - solve inequalities involving absolute value of linear expression <br> - solve system of linear inequalities in two variables by using graphical method <br> - solve quadratic inequalities by using product properties |


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|  | methods <br> - Apply Viete's theorem to solve related problems | - solve quadratic inequalities using the sign chart method. <br> - solve quadratic inequalities using graphs |
| III. SETS | - describe sets in different ways <br> - identify the elements of a given set <br> - explain the notion "empty set" and "universal set" <br> - determine the numbers of subsets of a given finite set and list them. <br> - give the power set of a given set <br> - determine the number of proper subsets of a given finite set and list them. <br> - distinguishes between equal sets and equivalent sets <br> - find equal sets and equivalent sets to a given set <br> - determine number of elements in the union of two finite set. <br> - describe the properties of "union" and "intersection" of sets. <br> - determine the absolute complement of a given set. <br> - determine the relative complement of two sets <br> - determine the symmetric difference of two sets. <br> - determine the Cartesian product of two sets. |  |
| IV. RELATION AND FUNCTION | - define the notions "relation", "domain" and "range" <br> - draw graphs of relations <br> - use graphs of relation to determine domain and range <br> - define function <br> - determine the domain and range of a given function. <br> - determine the sum difference, produced and quotient of functions. <br> - Evaluate combination of functions for a given values from their respective domain. <br> - sketch graphs of linear functions <br> - describe the properties of the graphs of linear functions. <br> - sketch the graphs of a given quadratic function. | - define the polynomial function of one variable <br> - identify the degree, leading coefficient and constant terms of a given polynomial functions. <br> - give different forms of polynomial functions <br> - perform the four fundamental operation on polynomials <br> - state and apply the polynomial division theorem <br> - state and apply the Factor Theorem <br> - determine the zero(s) of a given polynomial function <br> - state and apply the Location theorem to approximate the zero(s) of a given polynomial function |
| IV. RELATION AND | - describe the properties of the graphs of given quadratic | - apply the rational root test to determine the zero(s) |


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| FUNCTION (cont.) | functions <br> - determine the maximum and minimum values of a given quadratic function | of a given polynomial function. <br> - sketch the graph of a given polynomial function. <br> - describe the properties of the graphs of a given polynomial function <br> - explain what is meant by exponential expression <br> - state and apply the properties of exponents (where the exponents are real numbers) <br> - express what is meant by logarithmic expression by using the concept of exponential expression <br> - solve simple logarithmic equation by using the properties of logarithm <br> - recognize the advantage of using logarithm to the base 10 in calculation <br> - identify the "characteristics" and "mantissa" of a given common logarithm <br> - use the table for finding logarithm of a given positive number and antilogarithm of a number. <br> - compute using logarithm <br> - define an exponential function. <br> - draw the graph of a given exponential function <br> - describe the graphical relationship of exponential functions having bases reciprocal to each other <br> - describe the properties of an exponential function by using its graph. <br> - define a logarithmic function <br> - draw the graph of a given logarithmic function <br> - describe the properties of a logarithmic function by using its graph <br> - describe the graphical relationship of logarithmic function having bases reciprocal to each other. <br> - describe how the domains and ranges of $y=a^{x}$ and $y=\log _{a}{ }^{x}$ are related <br> - explain the relationship of the graphs of $y=a^{x}$ and $y=\log _{a}{ }^{x}$ |


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| IV. RELATION AND FUNCTION (cont.) |  | - solve equations involving exponents and logarithms as well <br> - solve problems, involving exponential and logarithmic functions, from real life. <br> - define the sine, cosine and tangent functions of an angle in the standard position. <br> - determine the values of the functions for an angle in the standard position, given the terminal side of that angle. <br> - determine the values of the sine, cosine and tangent functions for quadrantal angles <br> - locate negative and positive angles <br> - determine the values of trigonometric functions for some negative angles. <br> - determine the algebraic signs of the sine, cosine and tangent functions of angles in different quadrants. <br> - describe the relationship between trigonometrical values of complementary angles. <br> - describe the relationship between trignonometrical values of supplementary angles. <br> - determine the relationship between trigonometrical values of coterminal angles. <br> - determine the trigonometrical values of large angles <br> - construct a table of values for $y=\sin \theta$ where $-2 \pi$ $\leq \theta \leq 2 \pi$. <br> - draw the graph of $y=\sin \theta$ <br> - determine the domain range and period of the sine function. <br> - construct a table of values for $\mathrm{y}=\cos \theta$, where $2 \pi \leq \theta \leq 2 \pi$. <br> - draw the graph of $y=\cos \theta$ <br> - determine the domain, range and period of the cosine function. |


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| IV. RELATION AND FUNCTION (cont.) |  | - construct a table of values for $\mathrm{y}=\tan \theta$ where $-2 \pi$ $\leq \theta \leq 2 \pi$. <br> - draw the graph the tangent function $y=\tan \theta$. <br> - determine the domain, range and period of the tangent function. <br> - discuss the behavior of the graph of tangent function <br> - define the cosecant function <br> - determine the values of cosecant function for some angles. <br> - define the secant function. <br> - determine the values of secant function for some angles. <br> - define the cotangent function <br> - determine the values of cotangent function for some angles. <br> - explain the concept of co-functions. <br> - derive some of the trignometric identities. <br> - identity the quotient identities. <br> - solve problems related to trigonometrical identities. <br> - solve real life problems using trigonometircal ratios |
| V. STATISTICS AND PROBABILITY <br> Statistical Data | - differentiate primary and secondary data <br> - collect data from their environment <br> - classify and tabulate primary data according to the required criteria. <br> - construct a frequency distribution table for ungrouped data <br> - construct a histogram for a given data <br> - interprate a given histogram <br> - determine the Mean, Median and Mode of a given data <br> - describe the purposes and uses of Mean, Median and Mode <br> - identify the properties of the Mean of a given data (population function) <br> - compute the measures of dispersion for ungrouped data (manually and using scientific calculator) <br> - describe the purpose and use of measures of dispersion for |  |


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|  | ungrouped data. <br> - determine the probability of an event from a repeated experiment. <br> - determine the probability of an event. |  |
| VI. PLANE GEOMETRY AND MEASUREMENT <br> VI. PLANE GEOMETRY AND MEASUREMENT | - show that the sum of the measures of the interior angles of a triangle is $180^{\circ}$ <br> - find the measure of each interior angle of a regular polygon <br> - state properties of regular polygons. <br> - determine the lines of symmetry of regular polygons <br> - use the postulates and theorem on congruent triangle in solving related problems. <br> - define similar plane figures and similar solid figures. <br> - apply the SSS, SAS and AA similarity theorems to prove similarity of triangles <br> - discover the relationship between the perimeters of similar plane figures and use this relationship to solve related problems. <br> - discover the relationship between the areas of similar plane figures and use this' relationship to solve related problems. <br> - discover the relationship between the volumes of similar solid's and use this relationship to solve related problems. <br> - enlarge and reduce plane figures by a given scale factor. <br> - solve real life problems using the concepts of similarity and congruency. <br> - describe radian measure of an angle. <br> - convert radian measure to degree measure and vice versa. <br> - use the trigonometrical ratios to solve right angled triangles. <br> - find the angle whose trigonometrical value is given (using trigonometrical table. ) <br> - find the trigonemetrical values of angles from trigonometrical table. <br> - determine the trigonometrical values for obtuse angles using trigonometrical table. <br> - discover the symmetrical properties of circles <br> - use the symmetrical properties of circles to solve related problems | - derive the distance formula (to find distance between two points in the coordinate plane) <br> - apply the distance formula to solve related problems in the coordinates plane <br> - determine the coordinates of points that divide a given line segment in a given ratio <br> - define the gradient of a given line <br> - determine the gradient of a given line (given two points on the line) <br> - determine the equation of a given line <br> - identify whether to lines are parallel or not. <br> - identify whether two lines are perpendicular or not. <br> - apply the properties of the slopes of parallel and perpendicular lines to solve related problems <br> - apply the incidence theorems to solve related problems. <br> - apply theorems on special quadrilateral in solving related problems <br> - Apply the theorems on angles and arcs determined by lines intersecting inside, on and outside a circle to solve related problems <br> - calculate the perimeters of regular polygons <br> - calculate the areas of regular polygons <br> - apply the formulae for calculating surface area and volume of prism and cylinder <br> - calculate surface areas of a given pyramid or a cone <br> - calculate the volumes of a given pyramid or a cone. <br> - calculate the surface area of a given sphere |


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| (cont.) | - state angle properties of circles in their own words. <br> - apply angle properties of circles to solve related problems <br> - Find arc length, perimeters and areas of segments and sectors <br> - calculate areas of triangles using Heron's formula, whenever the lengths of the three sides only are given. <br> - calculate areas of parallelograms. <br> - Calculate the surface areas of cylinders and prisms. <br> - Calculate volumes of cylinders and prisms <br> - differentiate Vectors from scalars quantities. <br> - represent vectors pictorially <br> - explain what is meant by magnitude and direction of a vector. <br> - determine the sum of given vectors <br> - multiply a given vector by a given scales. <br> - express any given vector as position vector. | - calculate the volume of a given sphere <br> - define frustums of a pyramid and of a cone. <br> - calculate the surface areas of frustums of pyramids of cones. <br> - calculate the volumes of pyramids or of cones. <br> - determine the surface area of simple composed solids. <br> - calculate volumes of simple composed solids |

## Statement of Minimum Learning Competencies (MLCs) in Mathematics for Grade 11 \& 12

| Area of Competency | Grade 11 | Grade 12 |
| :---: | :---: | :---: |
| I. NUMBER SYSTEM <br> The set of Complex Number | - add complex numbers correctly <br> - subtract complex numbers correctly. <br> - describe the closure property of both addition and subtraction. <br> - describe the commutative and associative properties of complex numbers. <br> - identify the additive identity element in $\mathbb{C}$. <br> - determine the additive inverse of a given complex number. <br> - determine the product of two complex numbers. <br> - describe five basic properties of multiplication of complex numbers. <br> - divide two complex numbers <br> - give reason for each step in the process of division of complex numbers <br> - determine the conjugate of a given complex number. <br> - find the Modulus of any given complex number <br> - Write the simplified form of expressions involving complex numbers <br> - describe how to set up the Argand Plane. <br> - Plot the point corresponding to a given complex numbers. <br> - identify the complex number that corresponds to a given point in the Argand Plane. <br> - represent any complex number in the polar form <br> - determine the modulus and argument of a given complex number. |  |
| II. ALGEBRA <br> Rational Expression | - define rational expression <br> - identify the universal set of a given rational expression <br> - show the simplified form and the necessary steps in simplify a given rational expression <br> - Perform the four fundamental operations on rational expression |  |


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| Matrices and Determinants | - decompose rational expressions into sums of partial fractions. <br> - solve rational equations <br> - solve rational inequalities by using algebraic method (by considering all possible cases) <br> - solve rational inequality by using the sign chart method <br> - define matrix <br> - determine the sum and difference of two given matrices of the same order. <br> - multiply a matrix by a scalar <br> - describe the properties of multiplication of matrices by scalars. <br> - determine the product of two matrices. <br> - describe the properties of the product of two matrices. <br> - determine the transpose of a matrix <br> - determine the determinant of a square matrix of order 2. <br> - determine the minor and cofactor of a given element of a matrix <br> - calculate the determinate of a square matrix of order 3 . <br> - describe the properties of determinants. |  |
| II. ALGEBRA (cont.) |  |  |
| Matrices and Determinants (cont.) | - determine inverse of a square matrix <br> - find associated augmented matrix of equations <br> - describe elementary operations on matrices <br> - solve systems of equations in two or three variables using the elementary operations <br> - apply Cramer's rule to solve systems of linear equations |  |
| Introduction to Linear Programming | $\Rightarrow$ For social science stream only <br> - draw graphs of linear inequalities $\begin{aligned} & y \leq m x+c \text { and } \\ & y \geq m x+c \text { and } \\ & a x+b y \leq c \end{aligned}$ <br> - find maximum and minimum values of a given objective |  |


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|  | function under given constraints. <br> - create inequalities from real life examples for linear programming and solve the problem |  |
| II. ALGEBRA (cont.) <br> Mathematical Applications in Business | $\Rightarrow$ For social science stream only ( cont.) <br> - compare quantities in terms of ratio. <br> - calculate the rate of increase and the rate of decrease in price of commodities. <br> - solve problems on proportional variation in business <br> - solve problems on compound proportion <br> - find a required percentage of certain given amount <br> - compute problems on percentage increase or percentage decrease <br> - calculate payment by installment for a given simple interest arrangement. <br> - calculate the compound interest of a certain amount invested for a given period of time. <br> - apply the formula for compound interest to solve practical problems <br> - compute annuity for a give arrangement in compound interest. <br> - describe what is depreciation mean and some its causes <br> - compute depreciation by using either of the two methods appropriately. <br> - list five valid reasons for savings. <br> - explain how savings become investment. <br> - list three saving plans. <br> - identify four kinds of financial institutions. <br> - describe three main factors in choosing a particular institution for saving. <br> - identify the four factors that should guide consumers in planning an investment strategy. <br> - explain the differences between stocks and bond. <br> - describe ways to invest in stock and bond | $\Rightarrow$ For social science stream only <br> - find unit cost <br> - find the most economical purchase <br> - find total cost <br> - apply percent increase and percent decrease to business <br> - apply percent increase and percent decrease to business <br> - calculate initial expenses of buying a home <br> - calculate ongoing expenses of owing a home <br> - calculate commissions, total hourly wages, and salaries |
|  | $\Rightarrow$ For social science stream only ( cont.) |  |


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| II. ALGEBRA(cont.) <br> Mathematical Applications in Business | - describe the advantages and disadvantages of borrowing money <br> - identify the usual sources of cash loan.. <br> - compute the amount and time on the return of loan based on the or given agreement. <br> - name three types of activities that government performs and give examples of each <br> - explain why government collect taxes. <br> - describe the basic principles of taxation <br> - describe the various kinds of taxes. <br> - give their opinion about "income taxes" mean for them in relation to their future first job. <br> - calculate different types of taxes based on the "rate of tax" in Ethiopia |  |
| III. RELATION AND FUNCTION <br> Further on Relation and Function | - find out the inverse of a given relation <br> - Sketch the graph of a relation and its inverse. <br> - define power functions <br> - describe the properties of powers functions in relation to their exponents <br> - determine the domains and ranges of power functions <br> - sketch the graphs of power functions <br> - define Modulus Function (Absolute value Function, <br> - determine the domain and the range of modulus function <br> - sketch the graph of a Modulus function <br> - define the Signum function <br> - determine the domain and range of Signum function <br> - sketch the graph of the Signum function <br> - define the "Greatest Integer Function" <br> - determine the domain and range of the Greatest Integer function <br> - Sketch the graph of the Greatest Integer function <br> - define "one-to-one" function <br> - identify functions as one-to-one |  |


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|  | - define "on to' function <br> - identify functions as on to <br> - identify one-to-one correspondence <br> - define the composition of function. <br> - determine the composite function given the component functions <br> - determine the domain and the range of a composite function of two given functions. |  |
| III. RELATION AND <br> FUNCTION (cont.) <br> Further on Relation and Function | - define inverse function <br> - describe the condition for the existence of inverse function <br> - determine inverse function for an invertible function. <br> - determine whether two given functions are inverses of each other or not. <br> - Sketch the graph of the inverse of a function <br> - determine the domain and range of the inverse of a given function <br> - define rational function. <br> - determine the domain of a given rational function. <br> - determine the range of a given rational function. <br> - sketch the graph of a given rational function <br> - determine the intercepts and symmetry of the graph of a given rational function <br> - identify the type asymptote that the graph of a given function may have. <br> - tell the properties of a given rational function from its graph. <br> - use graphs of rational functions to solve rational inequalities |  |
| III. RELATION AND <br> FUNCTION (cont.) <br> Further on trigonometric | $\Rightarrow$ For Natural Science stream only <br> - define and describe the functions $\sec \mathrm{x}, \operatorname{cosec} \mathrm{x}$ and $\cot \mathrm{x}$. <br> - Sketch graphs of $\sec \mathrm{x}, \operatorname{cosec} \mathrm{x}$ and $\cot \mathrm{x}$ |  |


| Area of Competency | Grade 11 | Grade 12 |
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| functions | - define and describe the functions $\sec \mathrm{x}, \operatorname{cosec} \mathrm{x}$ and $\cot \mathrm{x}$. <br> - Sketch graphs of $\sec \mathrm{x}, \operatorname{cosec} \mathrm{x}$ and $\cot \mathrm{x}$ <br> - Sketch the graphs of $\begin{aligned} & y=a \sin x, \\ & y=a \sin k x ; \\ & y=a \sin (k x+b), \\ & y=a \sin (k x+b)+c \end{aligned}$ <br> - List the properties of these graphs. <br> - Sketch the graphs of $\begin{aligned} & y=a \cos x, \\ & y=a \cos k x \\ & y=a \cos (k x+b) \\ & y=a \cos (k x+b)+c \end{aligned}$ <br> - List the properties of these graphs. <br> - Apply trigonometric functions to solve problems from fields of science, navigation, engineering etc |  |
| III. RELATION AND FUNCTION (cont.) <br> Sequences and Series |  | - revise the notion of sets and functions. <br> - explain the concepts sequence, term of a sequence, rule (formula of a sequence) <br> - compute any term of a sequence using rule(formula). <br> - draw graphs of finite sequences. <br> - determine the sequence, use recurrence relations such as, $u_{n+1}=2 \mathbf{u}_{n}+1$, given $\mathbf{u}_{1}$ <br> - generate the Fibonacci sequence and investigate its uses, appearance in real life <br> - define arithmetic progressions and geometric progressions. <br> - Determine the terms of arithmetic and geometric sequences <br> - use the sigma notation for sums. <br> - compute partial sums of arithmetic and geometric progressions <br> - apply partial sum formula to solve problems of science and technology <br> - define a series |


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|  |  | - decide whether a given geometric series is divergent or convergent. <br> - show how infinite series can be divergent or convergent <br> - show how recurring decimals converge <br> - discuss the applications of arithmetic and geometric progressions (sequences) and series in science and technology and daily life. |
| IV. LOGIC <br> Mathematical Reasoning | - explain the difference between "statement" and "open statement" <br> - determine the truth value of a statement <br> - describe the rules for each of the five logical connectives. <br> - use the symbols $\neg, \wedge, \vee, \Rightarrow$ and $\Leftrightarrow$ to make compound statements <br> - determine truth values of compound statements connected by each of the logical connectives. <br> - determine truth values of two or three statements connected by two or three connectives <br> - describe the properties and laws of logical connectives <br> - determine the equivalence of two statements <br> - define "Contradiction and "Tautology" <br> - determine that a given compound statement is either a contradiction or tautology or neither of them <br> - find the "converse" of a given compound statement <br> - determine the truth value of the converse of a given compound statement <br> - find the "contra -positive" of a given statement <br> - determine the truth value of the contra- positive of a given statement | - recall what they have studied about statements and logical connectives in the previous grade <br> - revise open statement <br> - understand the concept of quantifiers <br> - determine truth values of statements with quantifiers. <br> - define argument and validity <br> - check the validity of a given argument <br> - use rules of inference to demonstrate the validity of a given argument <br> - distinguish between the nature of different types of mathematical proofs. <br> - apply the right type of proof to solve the required problem <br> - apply the principle of mathematical induction for proving <br> - identify a problem and determine whether it could be proved using principle of mathematical induction or not. |


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|  | - describe the two types of quantifiers <br> - determine the truth value of statements involving quantifiers <br> - describe what is meant by "argument" <br> - check the validity of a given argument <br> - use rules of inference to demonstrate the validity of a given argument. |  |
| V. STATISTICS AND PROBABILITY <br> Statistics and Probability | - identify qualitative and quantitative data <br> - describe the difference between discrete and continuous variables (data) <br> - identify ungrouped and grouped data <br> - determine class interval (class size) as required to form grouped data from a given ungrouped data <br> - make cumulative frequency table for grouped data (for both discrete and continuous) <br> - described terms related to grouped continuous data, i.e., class limit, class boundary, class interval and class midpoint. <br> - determine class limit, class boundary, class interval and class midpoint for grouped continuous data. <br> - find the mean of a given grouped data. <br> - find median grouped discrete data <br> - find median for grouped data (continuous variable) <br> - determine the mode of a given grouped data. <br> - identify data that are unimodal, bimodal and multimodal. <br> - determine the quartiles for a given grouped data <br> - determine the required deciles of a given frequency distribution <br> - determine the required percentile of a given frequency distribution. <br> - describe the dispersion of data values <br> - find the range of a given data. <br> - Compute variance for ungrouped data | - $\Rightarrow$ For social science stream only <br> - describe the three methods/techniques of sampling. <br> - explain the advantages and limitation of each techniques of sampling. <br> - describe the different ways of representations of data. <br> - explain the purpose of each representation of data. <br> - Construct graphs of statistical data <br> - identify statistical graph. <br> - explain the significance of representing a given data in different types of graphs. <br> - draw histogram for a given frequency distribution <br> - Sketch frequency polygon for a given frequency distribution <br> - sketch frequency curve for a given frequency distribution <br> - draw bar chart <br> - construct line graph for data related to time. <br> - construct pie chart for a given data. <br> - compute the three mean divations of a given data. <br> - describe the relative significance of Mean divation as a measure of dispersion. <br> - calculate the inter-quartile range for a given data. <br> - describe inter-quartile range as a measure of variability in values of a given set of data. <br> - describe the usefulness of standard deviation in interpreting the variability of a given data. |


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| V. STATISTICS AND PROBABILITY (cont.) <br> Statistics and Probability (cont.) | - calculate variance for grouped data. <br> - solve problems on variance <br> - Calculate standard deviation for grouped data. <br> - determine the number of different ways of possible selections from a given sets of objects (by using the multiplication principle) <br> - find the number of ways of selections of mutually exclusive operations (by using the addition principle) <br> - determine the factorial of a given non-negative integer <br> - find the possible ways of arranging objects by using the principle of permutation <br> - compute the possible arrangement of objects around the circle (using the principle of circular permutation) <br> - describe the difference between arrangement of objects and selection of objects. <br> - describe what is meant by "combination of objects" <br> - determine the number of different combinations of $\mathbf{n}$ objects, taken $\mathbf{r}$ at a time. <br> - explain the computational relationship between permutation and combination of objects. <br> - prove simple facts about combination. <br> - solve practical problems on combination of objects <br> - write up to the $6^{\text {th }}$ power of a binomial expression $(x+y)^{\mathrm{n}}$ (i.e. when $\mathrm{n}=0,1,2,3,4,5$ ) in its expanded form by using direct multiplication <br> - describe what they observe in the expansion of $(x+y)^{n}$ where $\mathrm{n}=0,1,2,3,4,5$ <br> - describe "Pascal's Triangle" and its use <br> - apply the "Binomial Theorem" in expanding the $\mathrm{n}^{\text {th }}$ power of binomial terms i.e. $(x+y)^{n}$, where $n \in \mathbf{Z}^{+}$ <br> - determine any term in the expanded form of $(x+y)^{n}$ where $\mathrm{n} \in \mathbf{Z}^{+}$solve problems on binomial expansion | $\Rightarrow$ For social science stream only ( cont. ) <br> - compare two groups of similar data.. <br> - determine the consistency of two similar group of data with equal mean but different standard deviations <br> - describe the application of coefficient of variation inn comparing two groups of similar data. <br> - describe the relationship among mean, median and mode for grouped data by using its frequency curve. <br> - use cumulative frequency graphs to determine the dispersion of values of data (interms of its Mean, Median and Standard deviation) <br> - determine the variability of value of data interms of quartiles by using cumulative frequency graph. <br> - describe the relationship among mean, median and mode for grouped data by using its frequency curve. |
| V. STATISTICS AND PROBABILITY (cont.) | - determine any term in the expanded form of $(x+y)^{\mathrm{n}}$, where $\mathrm{n} \in \mathbf{Z}^{+}$ <br> - solve problems on binomial expansion <br> - describe what is meant by "Random Experiment" <br> - explain what is meant by an outcome of a random |  |


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| Statistics and Probability (cont.) | experienced <br> - describe what is meant by sample space of a given random experiment. <br> - list some of the sample points of a sample space for a given experiment. <br> - define "equally likely outcomes" of a given trial in his own words. <br> - define "favorable outcomes/ cases" <br> - determine events of a given random experiment <br> - identify sample (elementary) events and compound events <br> - determine the number of events of a given sample space <br> - describe the occurrence or non occurrence of an event. <br> - explain an event denoted by "not $\mathbf{E}$ " where " $\mathbf{E}$ " is a given event <br> - explain events connected by "or" and "and" <br> - describe the simplified forms of events by using the properties of operations on sets <br> - identify exhaustive events <br> - identify mutually exclusive events <br> - describe events that are both exhaustive and mutually exclusive <br> - identify independent events. <br> - identify dependent events <br> - describe the axiomatic approach of probability <br> - interpret basic facts in the theory of probability. |  |
| V. STATISTICS AND PROBABILITY (cont.) <br> Statistics and Probability (cont.) | - find probabilities of events based on <br> - find probabilities of events based on "Axiomatic" approach. <br> - describe the odds infamous of an event or the odds against an event <br> - Find the probability of $\mathbf{E}_{\mathbf{1}} \cup \mathbf{E}_{\mathbf{2}}$ where $\mathbf{E}_{1}$ and $\mathbf{E}_{\mathbf{2}}$ are events in a random experiment <br> - determine the probability of mutually exclusive events. <br> - find probability of the joint occurrence independent event (by using rule of multiplication) <br> - describe the out comes of events using tree diagram <br> - determine the probability of the joint occurrence of |  |


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|  | dependent events (using multiplication rule) <br> - describe the outcomes of events using tree diagram to determine their probability <br> - identify whether a given events are independent or dependent (by comparing the equation for probability of joint occurrence of independent events). |  |
| VI. CALCULUS <br> Limits of sequence of numbers |  | - define upper and lower bound of number sequences. <br> - find out the least upper (greatest lower) bound of sequences. <br> - define limit of a number sequence <br> - consolidate their knowledge on the concept of sequences stressing on the concept of null sequence. <br> - apply theorems on the convergence of bounded sequences <br> - prove theorem about the limit of the sum of two convergent sequences. <br> - apply theorems on the limit of the difference, product, quotient of two convergent sequences <br> - define limit of a function. <br> - determine the limit of a given function at a point. <br> - find out the limit of the sum, difference, product and quotient of two functions. <br> - define continuity of a function in interval. <br> - describe the properties of continuous functions. <br> - use properties of continuous functions to determine the continuity of various functions. <br> - consolidate what they have studied on limits. <br> - solve problems on limit and continuity to stabilize what have learnt in the unit. |
| VI. CALCULUS |  | - find the rate of change of one quantity with respect to another. <br> - sketch different straight line and curved graphs and find out slopes at different points of each graph. <br> - define differentiability of a function at a point $x_{0}$. |


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| Introduction to Differential Calculus <br> Application of Differential Calculus |  | - explain the geometrical and mechanical meaning of derivative. <br> - set up the equation of tangent line at the point of tangency, using the concept of derivative. <br> - find the derivative of elementary functions over an interval. <br> - find the derivatives of power, simple trigonometric, exponential and logarithmic functions <br> - apply the sum and difference formulae of differentiation of functions. <br> - apply the product and quotient formulae of differentiation of functions. <br> - apply the chain rule and differentiate composition of functions <br> - find the $2^{\text {nd }}$ and the $\mathrm{n}^{\text {th }}$ derivative of a function. <br> - consolidate and stabilize what has been studied in the unit. <br> - consolidate the concept zero(s) of a function. <br> - find critical numbers and maximum and minimum values of a function on a closed interval. <br> - explain the geometric interpretations of Rolle's theorem and mean value theorem <br> - find numbers that satisfy the conclusions of mean value theorem and Rolle's theorem. <br> - Solve problems on application of differential calculus <br> - Interpret and apply differential calculus on problems involving the rate of change. <br> - consolidate what has been learnt in this unit |


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| Introduction to Integral Calculus |  | - differentiate between the concepts differentiation and integration <br> - use the properties of indefinite integrates in solving problems of integration <br> - integrate simple trigonometric functions <br> - use different techniques of integration for computation of integrals <br> - Compute area under a curve. <br> - use the concept of definite integral to calculate the area under a curve. <br> - state fundamental theorem of calculus <br> - apply fundamental theorem of calculus to solve integration problems. <br> - state the properties of definite integrals. <br> - apply the properties of definite integrals for computations of integration <br> - apply the knowledge on integral calculus to solve problems. |
| VII. GEOMETRY <br> Coordinate Geometry and Vectors | - write different forms of equation of a line. <br> - determine the slope, $x$-intercept and $y$-intercept of a line from its equation <br> - determine the angle between two intersecting lines on the coordinate plane whose equations are given. <br> - determine the distance between a point and a line given on the coordinates plane. <br> - name the different types of conic sections <br> - explain how the conic sections are generated (formed) <br> - define circle as a locus and write equation of a circle <br> - find the radius and center of a circle from its equation. <br> - determine whether a given line and circle have a point of intersection . <br> - determine the coordinates for the intersection point(s) (if the given line and the given circle intersect) <br> - write equation of a tangent line to a given circle. (where the point of tangency is given) | $\Rightarrow$ For social science stream only <br> - construct the coordinate axes in space <br> - identify planes determined by the axes in space. <br> - identify the octants determined by the planes and axes. <br> - read the coordinates of a point in space. <br> - describe how to locate a point in space. <br> - plot a point whose coordinates are given. <br> - give the equations for the planes determined by the axes. <br> - show graphically how to find the distance between two points in space. <br> - compute distance between two given points in space. <br> - determine coordinates of the mid-point of a segment in space. <br> - describe the equation of a sphere <br> - derive equation of a sphere |


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|  | - Write the standard form of equation of a parabola. <br> - draw different types of a parabolas <br> - describe some properties of a given parabola. <br> - define "ellipse" as a locus (set of points on the plane which satisfy a certain given condition) <br> - write the standard form of equation of an ellipse and sketch ellipse <br> - describe some terms related to ellipses ( such as latus rectum, eccentricity, major and minor axes...) <br> - define hyperbola as a locus <br> - write the standard form of equation of an ellipse <br> - describe related terms to hyperbola (foci, centre, transverse axis, asymptotes, conjugate axis...) <br> - sketch hyperbola based on its given equation <br> - give eccentricity of a given hyperbola solve problems on hyperbola | - solve problems related with sphere <br> - add, subtract vectors and multiply by a scalar in space <br> - use the unit vectors $\mathrm{i}, \mathrm{j}$ and k while representing a vector. <br> - describe the properties of addition to solve exercise problems.. <br> - show the closure property on their own <br> - find the length of a vector in space <br> - find the scalar product of two vectors in space. <br> - evaluate and show the angle between two vectors in space. |

