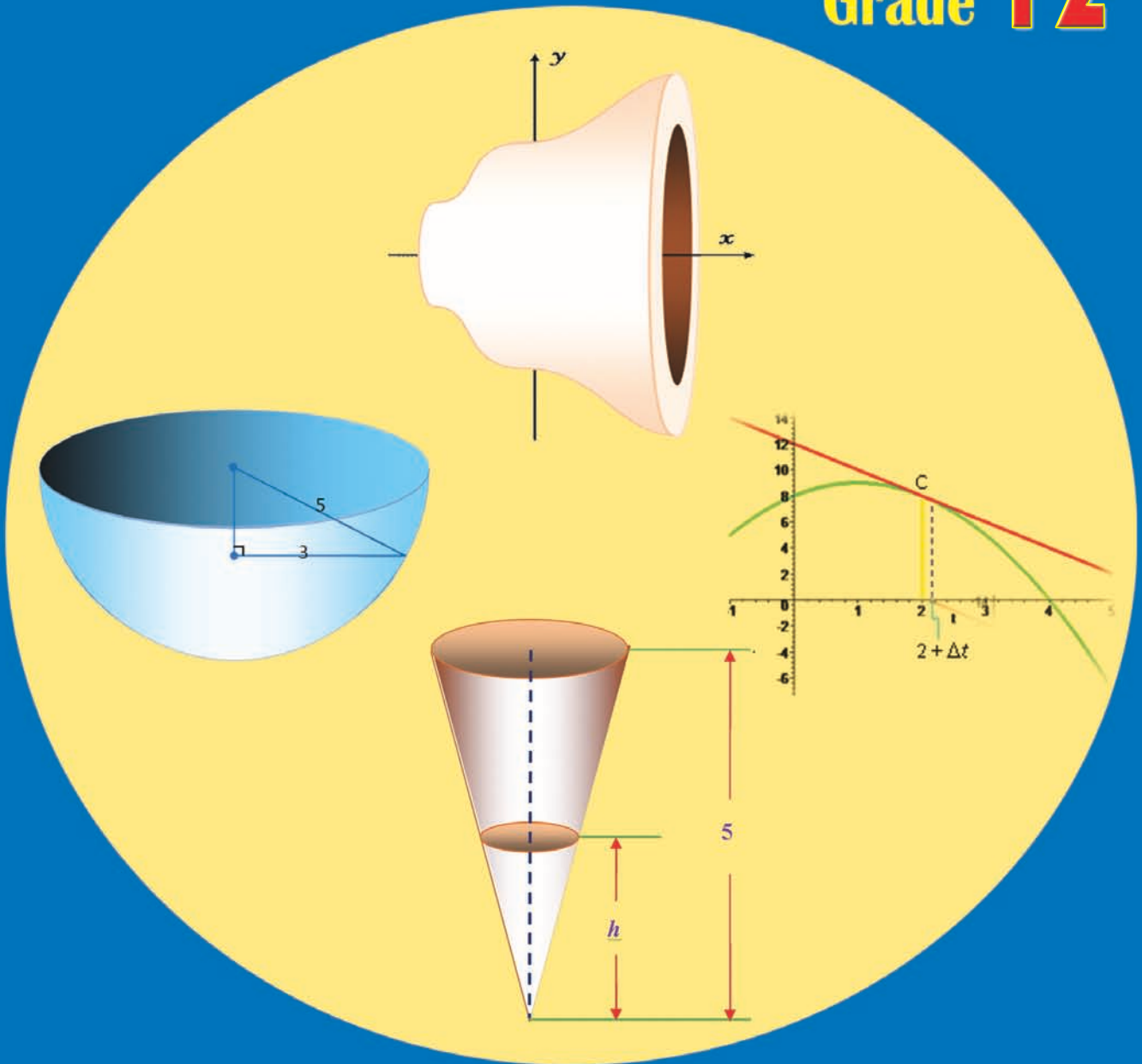




MATHEMATICS

STUDENT TEXTBOOK Grade 12



FEDERAL DEMOCRATIC REPUBLIC OF ETHIOPIA
MINISTRY OF EDUCATION

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MATHEMATICS

STUDENT TEXTBOOK

GRADE 12

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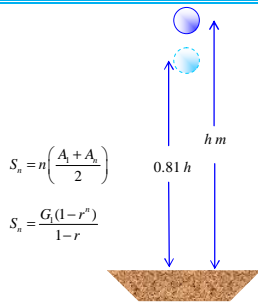
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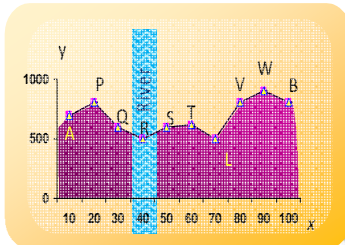
Contents

Unit 1 Sequences and Series 1



1.1	Sequences.....	3
1.2	Arithmetic sequences and geometric sequences.....	9
1.3	The sigma notation and partial sums.....	17
1.4	Infinities series	27
1.5	Applications of arithmetic progressions and geometric progressions.....	32
	<i>Key Terms</i>	37
	<i>Summary</i>	37
	<i>Review Exercises on Unit 1</i>	38

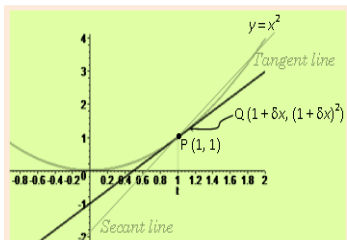
Unit 2 Introduction to Limits and Continuity..... 41



2.1	Limits of sequences of numbers	43
2.2	Limits of functions.....	60
2.3	Continuity of a function.....	76
2.4	Exercises on applications of limits	92
	<i>Key Terms</i>	98
	<i>Summary</i>	98
	<i>Review Exercises on Unit 2</i>	100

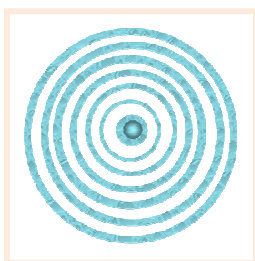


Unit 3 Introduction to Differential Calculus..... 103



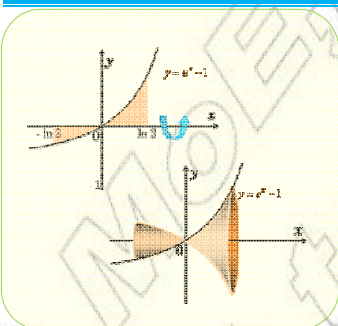
3.1	Introduction to Derivatives	104
3.2	Derivatives of some functions	121
3.3	Derivatives of combinations and compositions of functions	128
	<i>Key Terms</i>	155
	<i>Summary</i>	156
	<i>Review Exercises on Unit 3</i>	158

Unit 4 Applications of Differential Calculus 161



4.1	Extreme values of functions	163
4.2	Minimization and maximization problems...	189
4.3	Rate of change	197
	<i>Key Terms</i>	204
	<i>Summary</i>	204
	<i>Review Exercises on Unit 4</i>	206

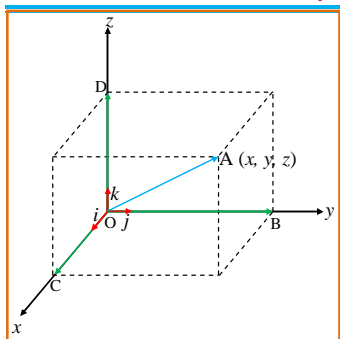
Unit 5 Introduction to Integral Calculus 207



5.1	Integration as reverse process of differentiation.....	208
5.2	Techniques of integration	220
5.3	Definite integrals, area and fundamental theorem of calculus	233
5.4	Applications of Integral calculus	245
	<i>Key Terms</i>	266
	<i>Summary</i>	266
	<i>Review Exercises on Unit 5</i>	268

Unit 6

Three Dimensional Geometry and Vectors in Space (For Natural Science Students) 271



6.1	Coordinate axes and coordinate planes in space.....	272
6.2	Coordinates of a point in space.....	274
6.3	Distance between two points in space.....	276
6.4	Mid-point of a line segment in space.....	280
6.5	Equation of sphere.....	282
6.6	Vectors in space.....	285
	<i>Key Terms</i>	293
	<i>Summary</i>	293
	<i>Review Exercises on Unit 6</i>	294

Unit 7

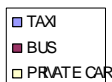
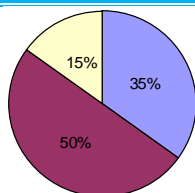
Mathematical Proofs (For Natural Science Students) 296

p	q	$p \Rightarrow q$	$(p \Rightarrow q) \wedge \neg q$	$[(p \Rightarrow q) \wedge \neg q] \Rightarrow \neg p$
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7.1	Revision on logic.....	297
7.2	Different types of proofs.....	307
7.3	Principle and application of mathematical induction.....	312
	<i>Key Terms</i>	317
	<i>Summary</i>	318
	<i>Review Exercises on Unit 7</i>	320

Unit 8 Further on Statistics

(For Social Science Students) 322



8.1	Sampling techniques	323
8.2	Representation of data	328
8.3	Construction and interpretation of graphs ..	332
8.4	Measures of central tendency and measures of variability	344
8.5	Analysis of frequency distributions.....	359
8.6	Use of cumulative frequency curves.....	362
	<i>Key Terms</i>	366
	<i>Summary</i>	366
	<i>Review Exercises on Unit 8</i>	368

Unit 9 Mathematical Applications for Business and consumers (For Social Science Students) 370



9.1	Applications to purchasing	371
9.2	Percent increase and percent decrease.....	373
9.3	Real estate expenses	380
9.4	Wages	385
	<i>Key Terms</i>	389
	<i>Summary</i>	389
	<i>Review Exercises on Unit 9</i>	390
	Table of monthly payments	392
	Table of random numbers	393